

## Use of spherical coordinates to evaluate three-dimensional facial changes after orthognathic surgery

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### ABSTRACT

**Purpose:** This study aimed to assess the three-dimensional (3D) facial changes after orthognathic surgery by evaluating the spherical coordinates of facial lines using 3D computed tomography (CT).

**Materials and Methods:** A 19-year-old girl was diagnosed with class III malocclusion and facial asymmetry. Orthognathic surgery was performed after orthodontic treatment. Facial CT scans were taken before and after orthognathic surgery. The patient had a menton deviation of 12.72 mm before surgery and 0.83 mm after surgery. The spherical coordinates of four bilateral facial lines (ramal height, ramal lateral, ramal posterior and mandibular body) were estimated from CT scans before and after surgery on the deviated and opposite side.

**Results:** The spherical coordinates of all facial lines changed after orthognathic surgery. Moreover, the bilateral differences of all facial lines changed after surgery, and no bilateral differences were zero.

**Conclusion:** The spherical coordinate system was useful to compare differences between the presurgical and post-surgical changes to facial lines. (*Imaging Sci Dent* 2014; 44 : 15-20)

**KEY WORDS:** Tomography, X-Ray Computed; Facial Asymmetry; Orthognathic Surgery

### Introduction

In many cases with class III malocclusion, orthognathic surgery is required to improve function and aesthetics with significant changes to hard and soft tissues.<sup>1-15</sup> One of the main purposes of orthognathic surgery is to create a symmetric face. Accurate diagnosis of facial asymmetry is not only essential for presurgical treatment planning but also for postsurgical evaluation. Three-dimensional (3D) computed tomography (CT) depicts the human face without

superimposition, magnification, and distortion of anatomic structures, which are inherent in two-dimensional (2D) cephalometric radiographs. Three-dimensional evaluation is valuable because postsurgical changes, including those not evident in that 2D imaging modalities, can be assessed. Improvements to facial symmetry may be more accurately assessing 3D modalities to evaluate facial changes after surgery than are 2D modalities.<sup>14,15</sup>

In the 3D analysis of facial asymmetry, the linear distances and angles among structures are commonly used.<sup>14-17</sup> A spherical coordinate system can be modified to analyze facial lines. Recently, a new spherical coordinate system for the 3D analysis of facial asymmetry was introduced. Using this new system, facial lines can be more clearly defined by their length as well as vertical and horizontal

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angle in the spherical coordinate system.<sup>18-20</sup> The spherical coordinate system may be used to indicate definitive changes to the facial area before and after orthognathic surgery.

The purpose of this study was to assess changes to the facial area of one patient with Class III malocclusion and significant facial asymmetry before and after orthognathic surgery by analyzing facial lines (spherical coordinate system) from 3D CT images.

## Materials and Methods

### Study subject

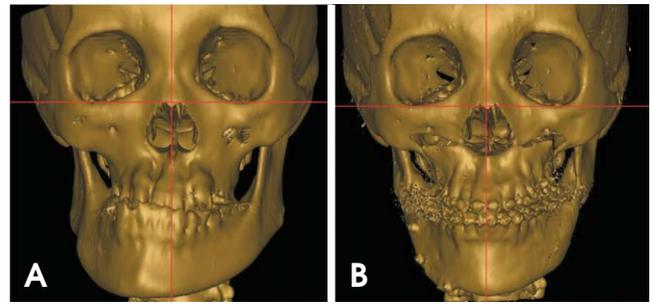
A 19-year-old female diagnosed with mandibular prognathism, maxillary hypoplasia, and lip canting was evaluated before and after orthognathic surgery via 3D CT. The orthognathic surgery included a mandibular setback, Le Fort I canting correction, and right mandibular angle reduction. The menton (Me) deviation was reduced from 12.72 mm to 0.83 mm after surgery, which was measured as the distance of Me from the midsagittal reference plane on the reconstructed 3D CT image.

### CT scans

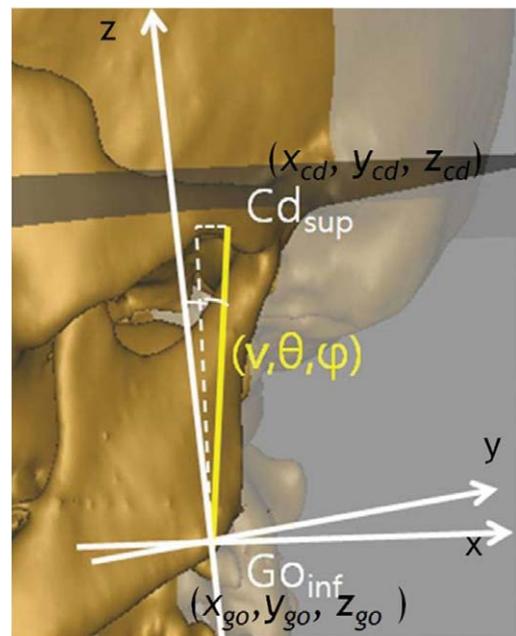
CT scans were obtained using a spiral CT scanner (Light Speed QX/I, GE Medical Systems, Milwaukee, WI, USA) with a  $512 \times 512$  matrix (120 kV, 200 mA, and a gantry angle of zero). The axial image thickness was 2.5 mm, the table speed was 3 mm/sec, and the scanning time was 0.8 sec. Digital imaging and communication in medicine images were created at a slice thickness of 1.0 mm. The acquired data from these images were input into a personal computer, and the CT data were used to construct 3D images with the software Vworks+Vsurgery (Cybermed, Seoul, Korea).

### Landmarks and facial lines

Three orthogonal reference planes, the horizontal ( $xy$  plane), midsagittal ( $yz$  plane), and coronal ( $xz$  plane) planes, were established. The horizontal reference plane was first established using the right Po, right Or, and left Or. The midsagittal reference plane was formed perpendicular to the horizontal reference plane and passing through Na and Op. The coronal reference plane was defined as perpendicular to both the midsagittal and the horizontal reference planes passing through Op. Next, the condylar landmarks were identified as the most superior ( $Cd_{sup}$ ), lateral ( $Cd_{lat}$ ),

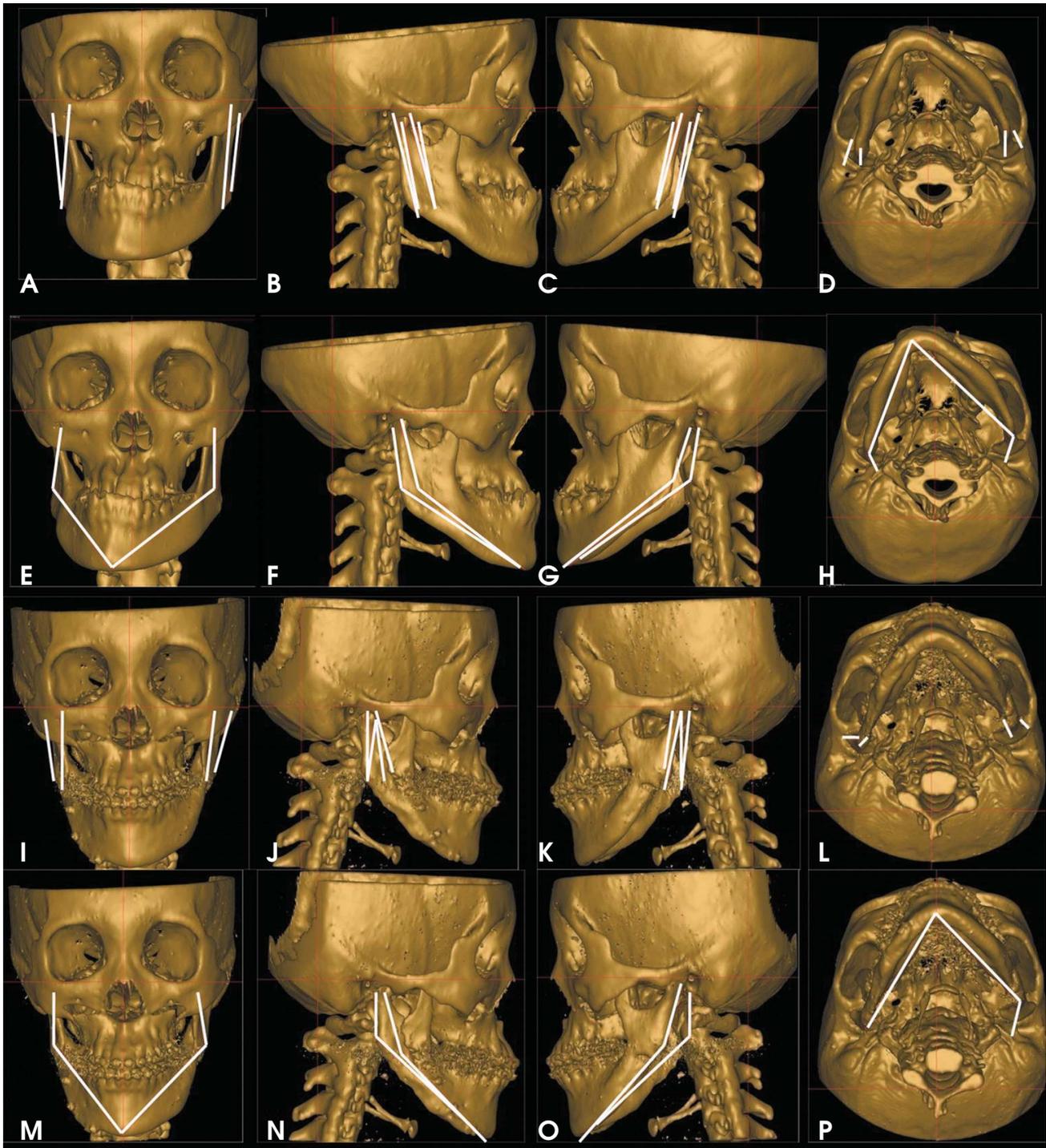


**Fig. 1.** CT scans from a 19-year-old female with class III malocclusion and facial asymmetry. A. Before orthognathic surgery. B. After orthognathic surgery. The menton deviation was reduced from 12.72 mm before surgery to 0.83 mm after surgery.



**Fig. 2.** A. Spherical coordinates of the analyzed facial lines and ramal height is shown. Length is indicated as  $v$ , the midsagittal inclination angle (between the line and the midsagittal reference plane) as  $\theta$ , and the coronal inclination angle (between the line and the coronal reference plane) as  $\phi$ .

and posterior ( $Cd_{post}$ ) points of the condylar head. The gonion landmarks were identified as the most inferior ( $Go_{inf}$ ), lateral ( $Go_{lat}$ ), and posterior ( $Go_{post}$ ) points of the gonion area. Additionally, the Me was defined as the most inferior point on the mandibular symphysis. The side of the face with the Me was identified as the deviated side, while the contralateral side of the face was considered the opposite side. The four facial lines that were established included the ramal height ( $Cd_{sup}-Go_{inf}$ ), ramal lateral ( $Cd_{lat}-Go_{lat}$ ), ramal posterior ( $Cd_{post}-Go_{post}$ ), and mandibular body ( $Go_{post}-Me$ ) with their respective landmarks. The spherical



**Fig. 3.** CT images of the facial lines before (A-H) and after (I-P) orthognathic surgery. A-D. The facial lines, ramal height and ramal lateral, before surgery. E-H. The facial lines, ramal posterior and mandibular body, before surgery. I-L. The facial lines, ramal height and ramal lateral, after surgery. M-P. The facial lines, ramal posterior and mandibular body, after surgery. The face remained three-dimensionally asymmetrical after surgery.

coordinates (length, midsagittal inclination angle, and coronal inclination angle) of the bilateral facial lines were mathematically calculated. Midsagittal and coronal inclination angles were considered the angles between the facial lines and midsagittal and coronal reference planes, respec-

tively. All postsurgical changes to the spherical coordinates were estimated on both the deviated and opposite side. Additionally, the bilateral differences among facial lines before and after surgery were evaluated (Figs. 1-3).<sup>19,20</sup>

**Table 1.** Spherical coordinates of facial lines before and after orthognathic surgery

Facial line	Face side	Spherical coordinate	Presurgical	Postsurgical	Difference
Ramal height (Cd <sub>sup</sub> -Go <sub>inf</sub> )	Deviated side	v	55.25	45.38	9.86
		θ	-1.96	4.18	-6.14
		φ	11.16	5.13	6.03
	Opposite side	v	58.16	42.59	15.57
		θ	0.44	3.49	-3.04
		φ	16.84	9.55	7.3
Ramal lateral (Cd <sub>lat</sub> -Go <sub>lat</sub> )	Deviated side	v	49.47	32.32	17.16
		θ	4.95	10.5	-5.55
		φ	10.27	-2.33	12.6
	Opposite side	v	46.73	31.66	15.07
		θ	7.41	12.48	-5.06
		φ	13.15	10.31	2.84
Ramal posterior (Cd <sub>Post</sub> -Go <sub>Post</sub> )	Deviated side	v	33.73	28.44	5.29
		θ	-5.48	1.19	-6.67
		φ	8.91	6.38	2.53
	Opposite side	v	37.44	32.25	5.19
		θ	-2.16	-2.58	0.42
		φ	17.83	16.39	1.45
Mandibular body (Go <sub>Post</sub> -Me)	Deviated side	v	93.5	94.2	-0.71
		θ	20.18	25.59	-5.41
		φ	56.87	48.44	8.42
	Opposite side	v	100.06	90.02	10.05
		θ	38.55	33.47	5.08
		φ	52.83	43.26	9.57

**Table 2.** Bilateral differences of facial lines before and after orthognathic surgery in the spherical coordinates

Facial line	Bilateral difference of spherical coordinates	Presurgical	Postsurgical	Difference
Ramal height (Cd <sub>sup</sub> -Go <sub>inf</sub> )	dv	-2.91	2.79	-5.7
	dθ	-2.4	0.7	-3.1
	dφ	-5.68	-4.41	-1.27
Ramal lateral (Cd <sub>lat</sub> -Go <sub>lat</sub> )	dv	2.75	0.66	2.09
	dθ	-2.46	-1.98	-0.49
	dφ	-2.88	-12.63	9.76
Ramal posterior (Cd <sub>Post</sub> -Go <sub>Post</sub> )	dv	-3.72	-3.81	0.09
	dθ	-3.32	3.77	-7.09
	dφ	-8.92	-10.01	1.08
Mandibular body (Go <sub>Post</sub> -Me)	dv	-6.57	4.19	-10.75
	dθ	-18.37	-7.88	-10.49
	dφ	4.03	5.18	-1.15

(dv, dθ, dφ)=spherical coordinates of deviated side-spherical coordinate of opposite side

### Results

The differences of length of facial lines (v) by surgery were between -0.71 mm and 17.16 mm. The differences of midsagittal inclination angle (θ) were between -6.67° and 5.08°. The differences of coronal inclination angle (φ) were between 1.45° and 12.60° (Table 1). The bilateral differences of the facial lines had changes after surgery. The changes of bilateral differences by surgery were between

-10.75 mm and 2.09 mm in length (dv), between -10.49° and -0.49° in midsagittal inclination angle (dθ), and between -1.27° and 9.76° in coronal inclination angle (dφ) (Table 2).

### Discussion

In this study, the spherical coordinate system was used to evaluate 3D facial changes after orthognathic surgery.

Spherical coordinate systems are used in various fields such as astronomy and geology. In geology, a spherical coordinate system is used to describe a flying object over the earth according to its distance from the center of the earth and its latitude and longitude. Similarly, the symmetry of human anatomical structures in 3D space can be also evaluated with the spherical coordinate system.<sup>18</sup> This system can be modified to define the length, midsagittal, and coronal inclinations of facial lines in 3D images of human structures.<sup>19,20</sup>

All spherical coordinates on both sides of the patient's face were three-dimensionally changed after orthognathic surgery (Table 1). In addition, the bilateral differences among all facial lines changed after surgery; however, the patient's face remained slightly asymmetric. No bilateral differences were zero. Although facial asymmetry was present after surgery, the bilateral differences were not consistent with the findings before surgery (Table 2).

Overall, this patient demonstrated a substantial reduction in facial asymmetry after surgery; the Me deviation, which is commonly used as an index to classify facial asymmetry,<sup>21,22</sup> decreased dramatically from 12.72 mm before surgery to 0.83 mm after surgery. If only the changes to the Me deviation are considered, facial asymmetry would be considered resolved in this subject. However, 3D analysis of the facial lines by the spherical coordinate system showed that the subject still had facial asymmetry after surgery. Facial asymmetry was resolved in the frontal plane; however, it remained after 3D CT analysis and all facial lines changed after surgery.

Previous reports have indicated that some level of asymmetry can remain after orthognathic surgery, yet surgery tended to result in facial lines that were within the normal range of facial symmetry.<sup>13,15</sup>

This study applied the spherical coordinate system to compare facial asymmetry before and after orthognathic surgery. The spherical coordinate substantially changed after surgery. This report suggests that facial asymmetry by surgery might not fully establish a 3D symmetric face in patients with facial asymmetry. Further investigation is required to compare 3D changes to spherical coordinates before and after surgery in a large sample size.

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